

EXEMPLO 5



A amostra 9, 8, 12, 7, 9, 6, 11, 6, 10, 9 foi extraída de uma população Normal. Construa um intervalo de confiança para a média ao nível de 95%.

Média amostral:

$$\bar{x} = \frac{\sum f_i \cdot x_i}{n} = \frac{2 \cdot 6 + 1 \cdot 7 + 1 \cdot 8 + 3 \cdot 9 + 1 \cdot 10 + 1 \cdot 11 + 1 \cdot 12}{10} = \frac{87}{10} = 8,7$$

$\alpha = 5\%$

x_i	f_i
6	2
7	1
8	1
9	3
10	1
11	1
12	1
total	10

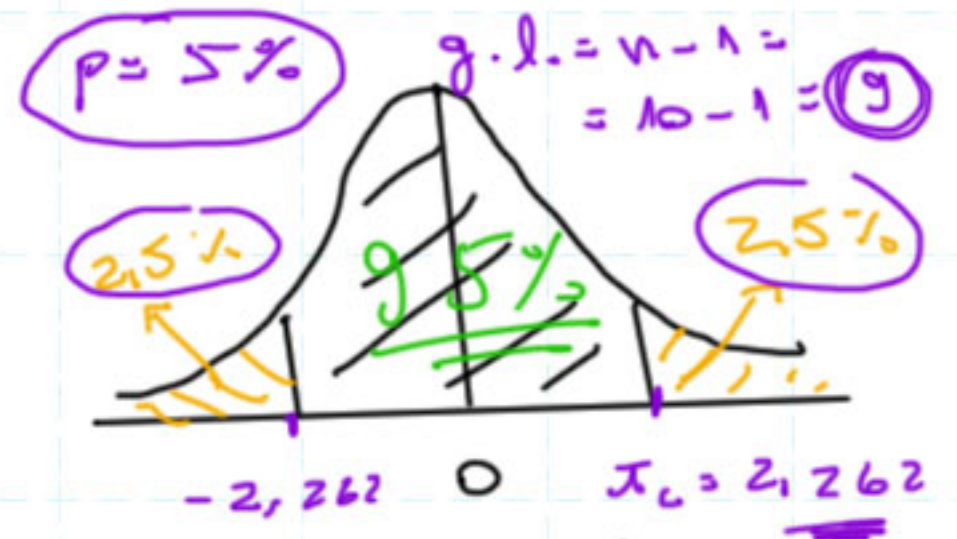
Variança amostral:

$$s^2 = \frac{\sum f_i (x_i - \bar{x})^2}{n-1} = \frac{2(6-8,7)^2 + 1(7-8,7)^2 + 1(8-8,7)^2 + 3(9-8,7)^2 + (10-8,7)^2 + (11-8,7)^2 + (12-8,7)^2}{10-1}$$

$$s = \sqrt{s^2} = \sqrt{\text{desvio padrão amostral}}$$

$$s = 2,00$$

$$n = 10$$



$$IC = \bar{x} \pm t_c \cdot \frac{s}{\sqrt{n}} = 8,7 \pm 2,262 \cdot \frac{2,00}{\sqrt{10}} = 8,7 \pm 1,43$$

$8,7 - 1,43 = 7,27$
 $8,7 + 1,43 = 10,13$

$$\therefore IC = [7,27 ; 10,13]$$

Distribuição t-Student: valores t_c tais que $P(-t_c \leq t \leq t_c) = 1 - p$

Graus de Liberdade

p ►	90%	80%	70%	60%	50%	40%	30%	20%	10%	8%	6%	5%	4%	2%	1%	0,2%	0,1%
1	0,158	0,325	0,510	0,727	1,000	1,376	1,963	3,078	6,314	7,916	10,579	12,706	15,895	31,821	63,657	318,309	636,619
2	0,142	0,289	0,445	0,617	0,816	1,061	1,386	1,886	2,920	3,320	3,896	4,303	4,849	6,965	9,925	22,327	31,599
3	0,137	0,277	0,424	0,584	0,765	0,978	1,250	1,638	2,353	2,605	2,951	3,182	3,482	4,541	5,841	10,215	12,924
4	0,134	0,271	0,414	0,569	0,741	0,941	1,190	1,533	2,132	2,333	2,601	2,776	2,999	3,747	4,604	7,173	8,610
5	0,132	0,267	0,408	0,559	0,727	0,920	1,156	1,476	2,015	2,191	2,422	2,571	2,757	3,365	4,032	5,893	6,869
6	0,131	0,265	0,404	0,553	0,718	0,906	1,134	1,440	1,943	2,104	2,313	2,447	2,612	3,143	3,707	5,208	5,959
7	0,130	0,263	0,402	0,549	0,711	0,896	1,119	1,415	1,895	2,046	2,241	2,365	2,517	2,998	3,499	4,785	5,408
8	0,130	0,262	0,399	0,546	0,706	0,889	1,108	1,397	1,860	2,004	2,189	2,306	2,449	2,896	3,355	4,501	5,041
9	0,129	0,261	0,398	0,543	0,703	0,883	1,100	1,383	1,833	1,973	2,150	2,262	2,398	2,821	3,250	4,297	4,781
10	0,129	0,260	0,397	0,542	0,700	0,879	1,093	1,372	1,812	1,948	2,120	2,228	2,359	2,764	3,169	4,144	4,587
11	0,129	0,260	0,396	0,540	0,697	0,876	1,088	1,363	1,796	1,928	2,096	2,201	2,328	2,718	3,106	4,025	4,437
12	0,128	0,259	0,395	0,539	0,695	0,873	1,083	1,356	1,782	1,912	2,076	2,179	2,303	2,681	3,055	3,930	4,318
13	0,128	0,259	0,394	0,538	0,694	0,870	1,079	1,350	1,771	1,899	2,060	2,160	2,282	2,650	3,012	3,852	4,221
14	0,128	0,258	0,393	0,537	0,692	0,868	1,076	1,345	1,761	1,887	2,046	2,145	2,264	2,624	2,977	3,787	4,140
15	0,128	0,258	0,393	0,536	0,691	0,866	1,074	1,341	1,753	1,878	2,034	2,131	2,249	2,602	2,947	3,733	4,073
16	0,128	0,258	0,392	0,535	0,690	0,865	1,071	1,337	1,746	1,869	2,024	2,120	2,235	2,583	2,921	3,686	4,015
17	0,128	0,257	0,392	0,534	0,689	0,863	1,069	1,333	1,740	1,862	2,015	2,110	2,224	2,567	2,898	3,646	3,965
18	0,127	0,257	0,392	0,534	0,688	0,862	1,067	1,330	1,734	1,855	2,007	2,101	2,214	2,552	2,878	3,610	3,922
19	0,127	0,257	0,391	0,533	0,688	0,861	1,066	1,328	1,729	1,850	2,000	2,093	2,205	2,539	2,861	3,579	3,883
20	0,127	0,257	0,391	0,533	0,687	0,860	1,064	1,325	1,725	1,844	1,994	2,086	2,197	2,528	2,845	3,552	3,850
21	0,127	0,257	0,391	0,532	0,686	0,859	1,063	1,323	1,721	1,840	1,988	2,080	2,189	2,518	2,831	3,527	3,819
22	0,127	0,256	0,390	0,532	0,686	0,858	1,061	1,321	1,717	1,835	1,983	2,074	2,183	2,508	2,819	3,505	3,792
23	0,127	0,256	0,390	0,532	0,685	0,858	1,060	1,319	1,714	1,832	1,978	2,069	2,177	2,500	2,807	3,485	3,768
24	0,127	0,256	0,390	0,531	0,685	0,857	1,059	1,318	1,711	1,828	1,974	2,064	2,172	2,492	2,797	3,467	3,745
25	0,127	0,256	0,390	0,531	0,684	0,856	1,058	1,316	1,708	1,825	1,970	2,060	2,167	2,485	2,787	3,450	3,725
26	0,127	0,256	0,390	0,531	0,684	0,856	1,058	1,315	1,706	1,822	1,967	2,056	2,162	2,479	2,779	3,435	3,707
27	0,127	0,256	0,389	0,531	0,684	0,855	1,057	1,314	1,703	1,819	1,963	2,052	2,158	2,473	2,771	3,421	3,690
28	0,127	0,256	0,389	0,530	0,683	0,855	1,056	1,313	1,701	1,817	1,960	2,048	2,154	2,467	2,763	3,408	3,674
29	0,127	0,256	0,389	0,530	0,683	0,854	1,055	1,311	1,699	1,814	1,957	2,045	2,150	2,462	2,756	3,396	3,659
30	0,127	0,256	0,389	0,530	0,683	0,854	1,055	1,310	1,697	1,812	1,955	2,042	2,147	2,457	2,750	3,385	3,646
31	0,127	0,256	0,389	0,530	0,682	0,853	1,054	1,309	1,696	1,810	1,952	2,040	2,144	2,453	2,744	3,375	3,633
32	0,127	0,255	0,389	0,530	0,682	0,853	1,054	1,309	1,694	1,808	1,950	2,037	2,141	2,449	2,738	3,365	3,622