

TESTE P/ MÉDIA COM VAR. DESCONHECIDA

↳ POP.

σ^2

Quando o desvio padrão σ for desconhecido, optamos por trabalhar com o desvio padrão amostral s . A estatística do teste se baseará na distribuição t de Student com (n-1) graus de liberdade:

$$t_{\text{obs}} = \frac{\bar{X} - \mu}{\frac{s}{\sqrt{n}}} \text{ com } \underline{\text{g.l.} = n-1}$$

onde:

\bar{X} é a média amostral;

μ é a média populacional testada (sob H_0);

s é o desvio padrão amostral;

n é o tamanho da amostra.



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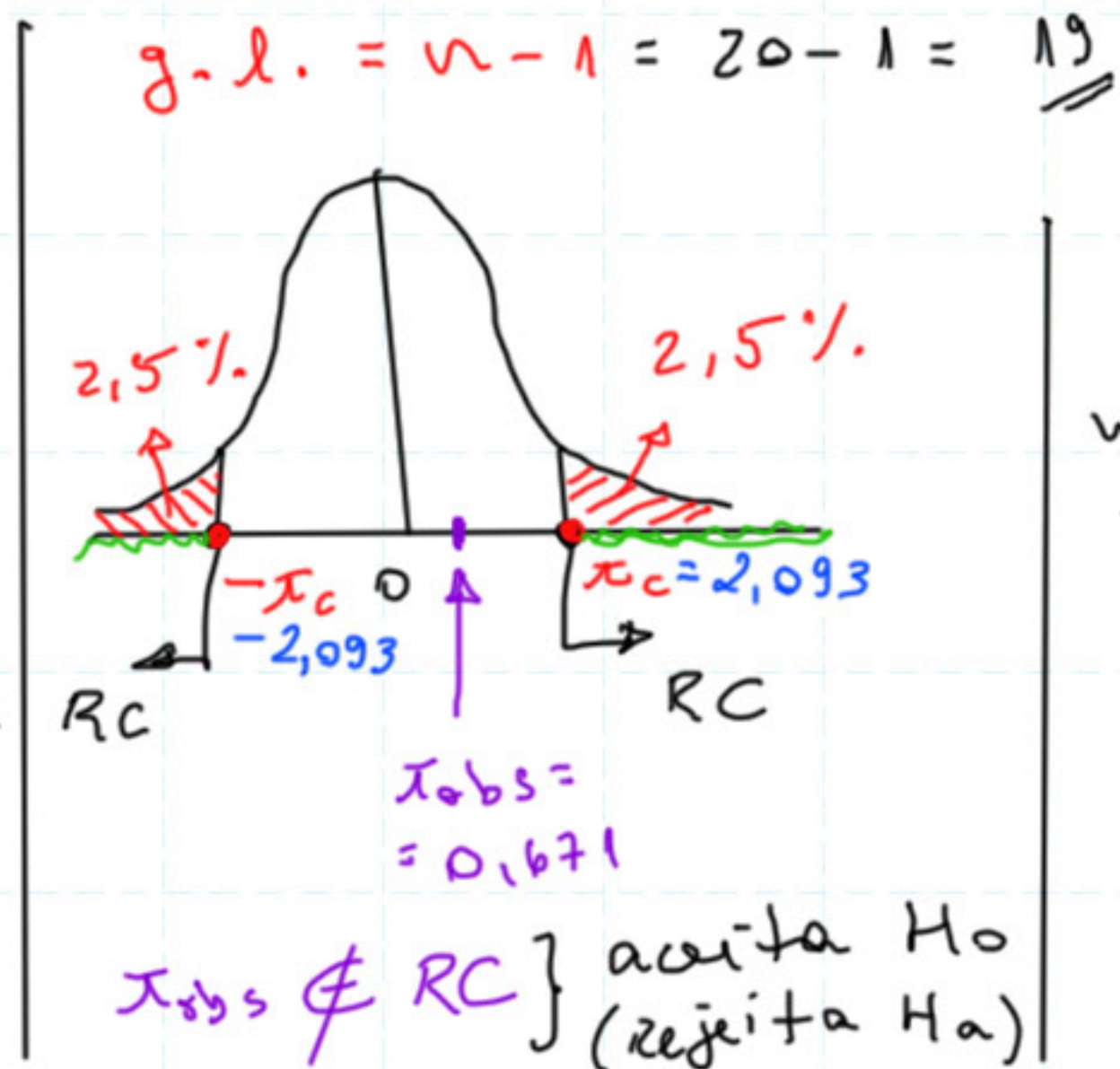
EXEMPLO 3

Os registros dos últimos anos de um colégio atestam para os calouros admitidos uma nota média 115 (teste vocacional). Para testar a hipótese de que a média de uma nova turma é a mesma das turmas anteriores, retirou-se uma amostra de 20 notas, obtendo-se média 118 e desvio padrão 20. Admita um nível de significância de 5% para efetuar o teste.

$n = 20$
 $\bar{x} = 118$
 $s = 20$

$H_0: \mu = 115$
 $H_a: \mu \neq 115$ *bilateral*

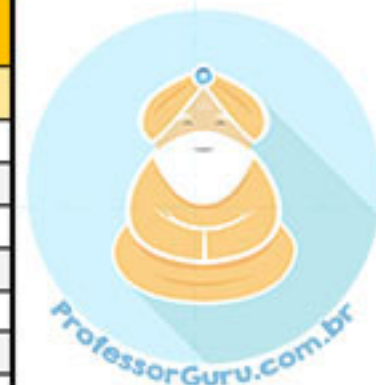
$$t_{obs} = \frac{\bar{x} - \mu}{\frac{s}{\sqrt{n}}} = \frac{118 - 115}{\frac{20}{\sqrt{20}}} = 0,671$$



$\alpha = 5\%$

At nível de 5%, não há evidências para se afirmar que a média mudou.

Distribuição t-Student: valores t_c tais que $P(-t_c \leq t \leq t_c) = 1 - p$



A+B



$p = 5\%$

Graus de Liberdade

p ▶	90%	80%	70%	60%	50%	40%	30%	20%	10%	8%	6%	5%	4%	2%	1%	0,2%	0,1%
1	0,158	0,325	0,510	0,727	1,000	1,376	1,963	3,078	6,314	7,916	10,579	12,706	15,895	31,821	63,657	318,309	636,619
2	0,142	0,289	0,445	0,617	0,816	1,061	1,386	1,886	2,920	3,320	3,896	4,303	4,849	6,965	9,925	22,327	31,599
3	0,137	0,277	0,424	0,584	0,765	0,978	1,250	1,638	2,353	2,605	2,951	3,182	3,482	4,541	5,841	10,215	12,924
4	0,134	0,271	0,414	0,569	0,741	0,941	1,190	1,533	2,132	2,333	2,601	2,776	2,999	3,747	4,604	7,173	8,610
5	0,132	0,267	0,408	0,559	0,727	0,920	1,156	1,476	2,015	2,191	2,422	2,571	2,757	3,365	4,032	5,893	6,869
6	0,131	0,265	0,404	0,553	0,718	0,906	1,134	1,440	1,943	2,104	2,313	2,447	2,612	3,143	3,707	5,208	5,959
7	0,130	0,263	0,402	0,549	0,711	0,896	1,119	1,415	1,895	2,046	2,241	2,365	2,517	2,998	3,499	4,785	5,408
8	0,130	0,262	0,399	0,546	0,706	0,889	1,108	1,397	1,860	2,004	2,189	2,306	2,449	2,896	3,355	4,501	5,041
9	0,129	0,261	0,398	0,543	0,703	0,883	1,100	1,383	1,833	1,973	2,150	2,262	2,398	2,821	3,250	4,297	4,781
10	0,129	0,260	0,397	0,542	0,700	0,879	1,093	1,372	1,812	1,948	2,120	2,228	2,359	2,764	3,169	4,144	4,587
11	0,129	0,260	0,396	0,540	0,697	0,876	1,088	1,363	1,796	1,928	2,096	2,201	2,328	2,718	3,106	4,025	4,437
12	0,128	0,259	0,395	0,539	0,695	0,873	1,083	1,356	1,782	1,912	2,076	2,179	2,303	2,681	3,055	3,930	4,318
13	0,128	0,259	0,394	0,538	0,694	0,870	1,079	1,350	1,771	1,899	2,060	2,160	2,282	2,650	3,012	3,852	4,221
14	0,128	0,258	0,393	0,537	0,692	0,868	1,076	1,345	1,761	1,887	2,046	2,145	2,264	2,624	2,977	3,787	4,140
15	0,128	0,258	0,393	0,536	0,691	0,866	1,074	1,341	1,753	1,878	2,034	2,131	2,249	2,602	2,947	3,733	4,073
16	0,128	0,258	0,392	0,535	0,690	0,865	1,071	1,337	1,746	1,869	2,024	2,120	2,235	2,583	2,921	3,686	4,015
17	0,128	0,257	0,392	0,534	0,689	0,863	1,069	1,333	1,740	1,862	2,015	2,110	2,224	2,567	2,898	3,646	3,965
18	0,127	0,257	0,392	0,534	0,688	0,862	1,067	1,330	1,734	1,855	2,007	2,101	2,214	2,552	2,878	3,610	3,922
19	0,127	0,257	0,391	0,533	0,688	0,861	1,066	1,328	1,729	1,850	2,000	2,093	2,205	2,539	2,861	3,579	3,883
20	0,127	0,257	0,391	0,533	0,687	0,860	1,064	1,325	1,725	1,844	1,994	2,086	2,197	2,528	2,845	3,552	3,850
21	0,127	0,257	0,391	0,532	0,686	0,859	1,063	1,323	1,721	1,840	1,988	2,080	2,189	2,518	2,831	3,527	3,819
22	0,127	0,256	0,390	0,532	0,686	0,858	1,061	1,321	1,717	1,835	1,983	2,074	2,183	2,508	2,819	3,505	3,792
23	0,127	0,256	0,390	0,532	0,685	0,858	1,060	1,319	1,714	1,832	1,978	2,069	2,177	2,500	2,807	3,485	3,768
24	0,127	0,256	0,390	0,531	0,685	0,857	1,059	1,318	1,711	1,828	1,974	2,064	2,172	2,492	2,797	3,467	3,745
25	0,127	0,256	0,390	0,531	0,684	0,856	1,058	1,316	1,708	1,825	1,970	2,060	2,167	2,485	2,787	3,450	3,725
26	0,127	0,256	0,390	0,531	0,684	0,856	1,058	1,315	1,706	1,822	1,967	2,056	2,162	2,479	2,779	3,435	3,707
27	0,127	0,256	0,389	0,531	0,684	0,855	1,057	1,314	1,703	1,819	1,963	2,052	2,158	2,473	2,771	3,421	3,690
28	0,127	0,256	0,389	0,530	0,683	0,855	1,056	1,313	1,701	1,817	1,960	2,048	2,154	2,467	2,763	3,408	3,674
29	0,127	0,256	0,389	0,530	0,683	0,854	1,055	1,311	1,699	1,814	1,957	2,045	2,150	2,462	2,756	3,396	3,659
30	0,127	0,256	0,389	0,530	0,683	0,854	1,055	1,310	1,697	1,812	1,955	2,042	2,147	2,457	2,750	3,385	3,646
31	0,127	0,256	0,389	0,530	0,682	0,853	1,054	1,309	1,696	1,810	1,952	2,040	2,144	2,453	2,744	3,375	3,633
32	0,127	0,255	0,389	0,530	0,682	0,853	1,054	1,309	1,694	1,808	1,950	2,037	2,141	2,449	2,738	3,365	3,622
33	0,127	0,255	0,389	0,530	0,682	0,853	1,053	1,308	1,692	1,806	1,948	2,035	2,138	2,445	2,733	3,356	3,611
34	0,127	0,255	0,389	0,529	0,682	0,852	1,052	1,307	1,691	1,805	1,946	2,032	2,136	2,441	2,728	3,348	3,601
35	0,127	0,255	0,388	0,529	0,682	0,852	1,052	1,306	1,690	1,803	1,944	2,030	2,133	2,438	2,724	3,340	3,591
36	0,127	0,255	0,388	0,529	0,681	0,852	1,052	1,306	1,688	1,802	1,942	2,028	2,131	2,434	2,719	3,333	3,582
37	0,127	0,255	0,388	0,529	0,681	0,851	1,051	1,305	1,687	1,800	1,940	2,026	2,129	2,431	2,715	3,326	3,574
38	0,127	0,255	0,388	0,529	0,681	0,851	1,051	1,304	1,686	1,799	1,939	2,024	2,127	2,429	2,712	3,319	3,566
39	0,126	0,255	0,388	0,529	0,681	0,851	1,050	1,304	1,685	1,798	1,937	2,023	2,125	2,426	2,708	3,313	3,558
40	0,126	0,255	0,388	0,529	0,681	0,851	1,050	1,303	1,684	1,796	1,936	2,021	2,123	2,423	2,704	3,307	3,551
45	0,126	0,255	0,388	0,528	0,680	0,850	1,049	1,301	1,679	1,791	1,929	2,014	2,115	2,412	2,690	3,281	3,520
50	0,126	0,255	0,388	0,528	0,679	0,849	1,047	1,299	1,676	1,787	1,924	2,009	2,109	2,403	2,678	3,261	3,496